

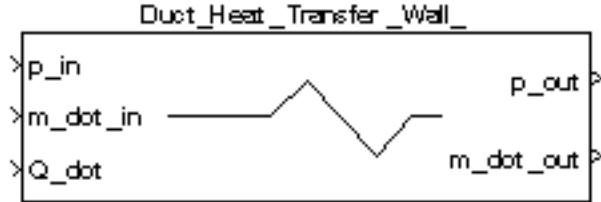
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## **Simulink Report: Duct\_Heat\_Transfer\_Wall\_**

Christian Müller

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# Model - Duct\_Heat\_Transfer\_Wall\_



**Tabelle 1.1. Duct\_Heat\_Transfer\_Wall\_ Simulation Parameters**

Solver ode14x	ZeroCross on	StartTime 0.0 StopTime 10.0
RelTol 1e-3	AbsTol auto	Refine 1
InitialStep auto	FixedStep auto	MaxStep auto

**Tabelle 1.2. Duct\_Heat\_Transfer\_Wall\_ Summary Information**

NumModelInputs	N/A	NumModelOutputs	N/A
NumVirtualSubsystems	N/A	NumNonvirtSubsystems	N/A
NumNonVirtBlocksInModel	N/A	NumBlockTypeCounts	N/A
NumBlockSignals	N/A	NumBlockParams	N/A
NumZCEvents	N/A	NumNonsampledZCs	N/A

## Systems

Name	Parent	Snapshot	Blocks	Signals
Duct_Heat_T ransfer_Wall_	<root>		Duct_Heat_Transfer_Wall_	Duct_Heat_Transfer_Wall_ <1> Duct_Heat_Transfer_Wall_ <2>

## Blocks

**Tabelle 1.3. Block Type Count**

BlockType	Count	Block Names
Import	69	p_in1, m_dot_in1, Q_dot, L, D_major, D_minor, In_1, In_2, L, n_unit, D_major, D_minor, b_wall, b_isolation, rho_wall, rho_isolation, c_wall, c_isolation, lambda_wall, lambda_isolation, L, zeta, mode, p_in_1, rho_in_1,

BlockType	Count	Block Names
		T_in_1, x_H2O_gas_in_1, x_CO2_in_1, x_H2O_liq_in_1, p_in_2, rho_in_2, T_in_2, x_H2O_gas_in_2, x_CO2_in_2, x_H2O_liq_in_2, T_wall, T_ambient, In_1, In_2, Q_dot, V, V, p_init, T_init, x_H2O_gas_init, x_CO2_init, x_H2O_liq_init, T, m_air, m_H2O_gas, m_CO2, m_H2O_liq, T_in_1, m_dot_air_in_1, x_H2O_gas_in_1, x_CO2_in_1, x_H2O_liq_in_1, T_in_2, m_dot_air_in_2, x_H2O_gas_in_2, x_CO2_in_2, x_H2O_liq_in_2, Q_dot, T, m_air, m_H2O_gas, m_CO2, m_H2O_liq, V
Outport	32	V, rho, T, x_H2O_gas, x_CO2, x_H2O_liq, p_1, m_dot_air_1, p_2, m_dot_air_2, Q_dot_fluid, T_dot_wall, Out_1, Out_2, Q_dot_fluid, m_air_init, m_H2O_gas_init, m_CO2_init, m_H2O_liq_init, T_dot, m_dot_air, m_dot_H2O_gas, m_dot_CO2, m_dot_H2O_liq, p, rho, x_H2O_gas, x_CO2, x_H2O_liq, Out, p_out1, m_dot_out1
Constant	24	D_major, D_minor, Constant2, D_major, D_minor, T_ambient, b_isolation, b_wall, c_isolation, c_wall, lambda_isolation, lambda_wall, mode, n_unit, rho_isolation, rho_wall, zeta, L, T_init, m_dot_air, p_init, x_CO2_init, x_H2O_gas_init, x_H2O_liq_init
Integrator	6	Integrator, Integrator1, Integrator2, Integrator3, Integrator4, Integrator5
Terminator	5	Terminator , Terminator , Terminator , Terminator , Terminator
Stateflow (m)	5	Embedded MATLAB Function, Embedded MATLA Function, Embedded MATLAB Function, Embedded_MATLAB_Function_1, Embedded_MATLAB_Function_2
S-Function	5	SFunction , SFunction , SFunction , SFunction , SFunction
Demux	5	Demux , Demux , Demux , Demux , Demux
BusSelector	4	Bus Selector3, Bus Selector4, Bus Selector2, Bus Selector5
SubSystem	3	Duct_Heat_Transfer_Wall_, FR, Vol_2D
BusCreator	3	Bus Creator1, Bus Creator2, Bus Creator1
Sum	1	Sum

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Function Block Parameters: Duct\_Heat\_Transfer\_Wall\_

Subsystem (mask)

Parameters

Number of identical Units  
1

Length Major Axis [m]  
NaN

Length Minor Axis [m]  
NaN

Length [m]  
NaN

Thickness Wall [m]  
NaN

Thickness Isolation [m]  
NaN

Density Wall [kg/m<sup>3</sup>]  
NaN

Density Isolation [kg/m<sup>3</sup>]  
NaN

Specific Heat Capacity Wall [J/kg/K]  
NaN

Specific Heat Capacity Isolation [J/kg/K]  
NaN

Thermal Conductivity Wall [J/s/m/K]  
NaN

Thermal Conductivity Isolation [J/s/m/K]  
NaN

Ambient Temperature [K]  
NaN

Initial Parameter: Temperature Wall [K]  
NaN

Initial Parameter: Pressure [Pa]  
NaN

Initial Parameter: Temperature [K]  
NaN

Initial Parameter: Water Vapor Content  
NaN

Initial Parameter: CO<sub>2</sub> Content  
NaN

Initial Parameter: Water Content  
NaN

Minor Loss Coefficient  
NaN

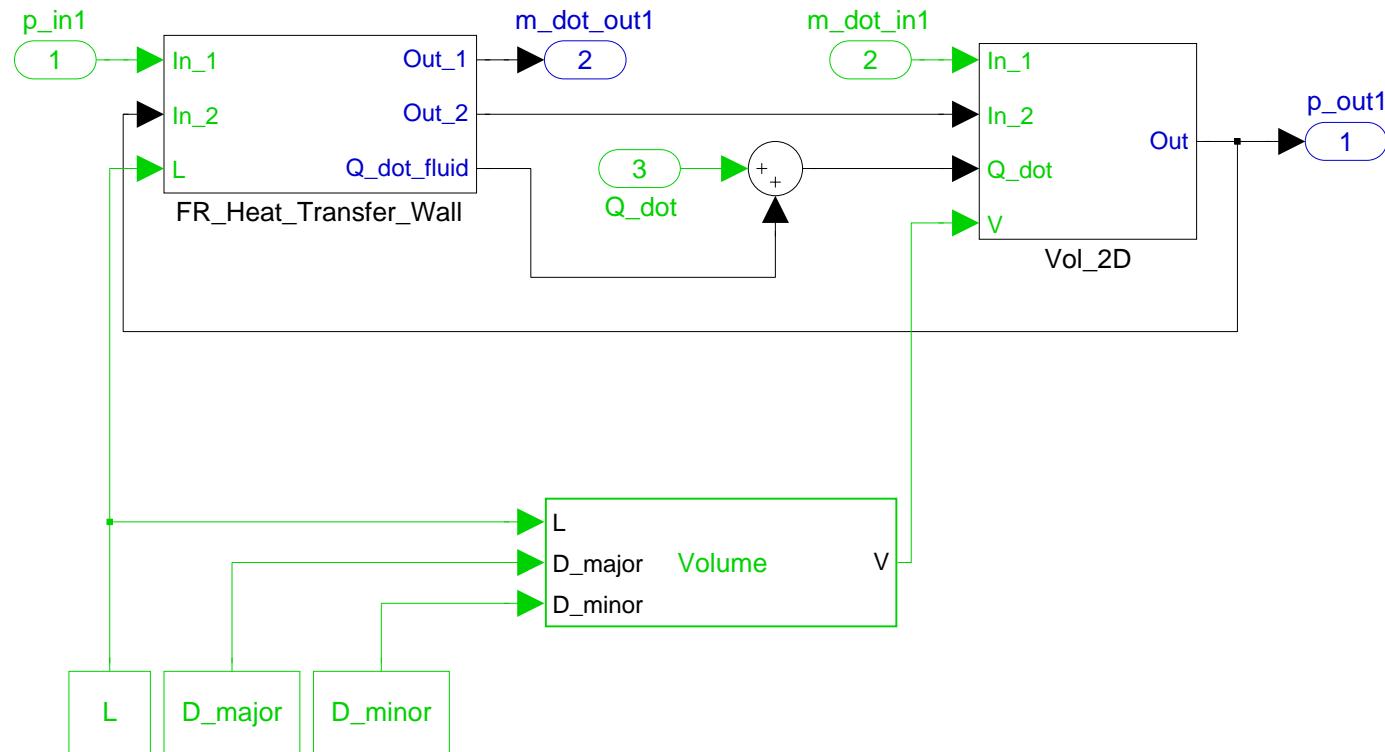
Mode = 0: State Variables = Average Input variables, Mode = 1: State Variables = Input Variables Higher Pressure  
NaN

OK

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```
function [rho,T,x_H2O_gas,x_CO2,x_H2O_liq,p_1,m_dot_air_1,p_2,m_dot_air_2,Q_dot_fluid,↵
T_dot_wall]=Cal(n_unit,D_major,D_minor,b_wall,b_isolation,rho_wall,rho_isolation,↵
c_wall,c_isolation,lambda_wall,lambda_isolation,L,zeta,mode,p_in_1,rho_in_1,T_in_1,↵
x_H2O_gas_in_1,x_CO2_in_1,x_H2O_liq_in_1,p_in_2,rho_in_2,T_in_2,x_H2O_gas_in_2,↵
x_CO2_in_2,x_H2O_liq_in_2,T_wall,T_ambient)

% ****
% * Definition of a flow resistance with heat transfer via wall
% *
% * Number of inputs : 2
% *
% * Parameter: Diameter: D
% * Length: L
% * Minor loss coefficient: zeta
% *
% *
% * Relevant input variables of Duct_Heat_Transfer_Wall
% *
% * Pressure: p_in
% * Density: rho_in
% * Temperature: T_in
% * Content water vapor: x_H2O_gas_in
% * Content CO2: x_CO2_in
% * Content water: x_H2O_liq_in
% *
% *
% * Relevant output variables of Duct_Heat_Transfer_Wall
% *
% * Temperature: T
% * Mass flow dry air: m_dot_air
% * Content water vapor: x_H2O_gas
% * Content CO2: x_CO2
% * Content water: x_H2O_liq
% *
% ****
% * Embedded Matlab Function Cal:
% *
% * Calculations:
% * 1. Calculation parameter.
% * 2. Calculation of the state variables.
% * 3. Calculation average viscosity.
% * 4. Calculation flow velocity.
% * 4.1 Initial value of the flow velocity.
% * 5. Calculation mass flow.
% * 6. Calculation heat transfer.
% *
% *
% * Assumptions:
% * 2. Mode = 0: state variables = average input variables
% * Mode = 1: state variables = input variables higher pressure
% * 3. The gas mixture inside the volume consists of water vapor (H2O_gas),
% * CO2 and water (H2O_liq, state: fog).
% * 4. The intial value of the flow velocity is estimated by the law of
% * Hagen-Poiseuille. Knowing the initial value of the velocity, the
% * initial value of the Reynolds number can be calculated. The iterative
% * while loop has a break condition of |v_(i-1)-v_(i)| < 0.001*v_(i-1).
```

```

% *      The input pressures are cross linked. p_in_1 is transferred to the output
% *      p_1 and the other way around.
% * 5. The mass flow is calculated with a incompressible mass flow equation.
% *      This equation is only applicable for systems with low flow velocities.
% * 6. a) Heat transfer fluid/wall (convection)
% *      b) Heat transfer wall/isolation (conduction)
% *      c) Heat transfer isolation/enviroment (conduction)
% *
% *
% * Last modification : 15.03.2008
% * Author : Christian Müller(HAW)
% *
% ****
% * 1. Calculation parameter
D_major           = abs(D_major);
D_minor           = abs(D_minor);

if D_major == D_minor
    A             = (pi/4)*D_major*D_minor;
    U_inner_duct   = pi*D_major;
    U_outer_duct   = pi*(D_major+b_wall);
    U_outer_isolation = pi*(D_major+b_wall+b_isolation);
    D             = U_inner_duct/pi;
else
    A             = (pi/4)*D_major*D_minor;
    K             = abs(D_major-D_minor)/(D_major+D_minor);
    U_inner_duct   = (D_major+D_minor)*pi*(1+(3*K^2)/(10+sqrt(4-3*K^2)));
    K             = abs((D_major+b_wall)-(D_minor+b_wall))/((D_major+b_wall)+
(D_minor+b_wall));
    U_outer_duct   = ((D_major+b_wall)+(D_minor+b_wall))*pi*(1+(3*K^2)/(10+sqrt(4-
3*K^2)));
    K             = abs((D_major+b_wall+b_isolation)-(D_minor+b_wall+b_isolation))/
((D_major+b_wall+b_isolation)+(D_minor+b_wall+b_isolation));
    U_outer_isolation = ((D_major+b_wall+b_isolation)+(D_minor+b_wall+b_isolation))*pi*(
1+(3*K^2)/(10+sqrt(4-3*K^2)));
    D             = U_inner_duct/pi;
end
% ****

% * 2. Calculation of the state variables.
rho               = 0;
T                 = 0;
x_H2O_gas         = 0;
x_CO2             = 0;
x_H2O_liq          = 0;

if mode == 0
    rho           = (rho_in_1+rho_in_2)/2;
    T             = (T_in_1+T_in_2)/2;
    x_H2O_gas     = (x_H2O_gas_in_1+x_H2O_gas_in_2)/2;
    x_CO2          = (x_CO2_in_1+x_CO2_in_2)/2;
    x_H2O_liq      = (x_H2O_liq_in_1+x_H2O_liq_in_2)/2;
end

if mode == 1

```

```

if p_in_1 >= p_in_2
    rho          = rho_in_1;
    T            = T_in_1;
    x_H2O_gas   = x_H2O_gas_in_1;
    x_CO2        = x_CO2_in_1;
    x_H2O_liq   = x_H2O_liq_in_1;
else
    rho          = rho_in_2;
    T            = T_in_2;
    x_H2O_gas   = x_H2O_gas_in_2;
    x_CO2        = x_CO2_in_2;
    x_H2O_liq   = x_H2O_liq_in_2;
end
end
% ****
%
% * 3. Calculation average viscosity.
eta_air      = 0.0000182;
eta_H2O_gas  = 0.00000877;
eta_CO2       = 0.0000149;
eta          = (eta_air+x_H2O_gas*eta_H2O_gas+x_CO2*eta_CO2) / %
(1+x_H2O_gas+x_CO2);
eta_kin      = eta/rho;
% ****
%
% * 4. Calculation flow velocity
% * 4.1 Initial value of the flow velocity.
p_1          = p_in_2;
p_2          = p_in_1;
Delta_p      = p_in_1-p_in_2;
V_dot        = ((pi*(D/2)^4)*abs(Delta_p))/(8*eta*L);
v            = V_dot/A;
Re           = (v*D)/eta_kin;
% ****
%
if Re < 1
    Re          = 1;
end
check        = 1;
while check > 0
    if Re<1187.384382
        lambda     = 64/Re;
        zeta_total = lambda*(L/D)+zeta;
        Z_v        = sqrt(abs(Delta_p)*(2/rho)*(1/zeta_total));
        if abs(v-Z_v) > (0.001*v)
            check    = 1;
        else
            check    = 0;
        end
    end
end

```

```

v           = Z_v;
Re          = (v*D)/eta_kin;

if Re < 1
    Re      = 1;
end
else
    lambda   = 0.3164*((Re)^(-0.25));
    zeta_total = lambda*(L/D)+zeta;
    Z_v       = sqrt(abs(Delta_p)*(2/rho)*(1/zeta_total));

    if abs(v-Z_v) > (0.001*v)
        check   = 1;
    else
        check   = 0;
    end

    v           = Z_v;
    Re          = (v*D)/eta_kin;
end
% ****

% * 5. Calculation mass flow
m_dot         = n_unit*A*rho*v;

if Delta_p>=0
    m_dot_air_1     = -m_dot*(1-((x_H2O_gas+x_CO2)/(1+x_H2O_gas+x_CO2)));
    m_dot_air_2     = m_dot*(1-((x_H2O_gas+x_CO2)/(1+x_H2O_gas+x_CO2)));
else
    m_dot_air_1     = m_dot*(1-((x_H2O_gas+x_CO2)/(1+x_H2O_gas+x_CO2)));
    m_dot_air_2     = -m_dot*(1-((x_H2O_gas+x_CO2)/(1+x_H2O_gas+x_CO2)));
end
% ****

% * 6. Calculation heat transfer
c_p_air        = 1005;
c_p_H2O_gas    = 1870;
c_p_CO2        = 830;
c_p            = (c_p_air+x_H2O_gas*c_p_H2O_gas+x_CO2*c_p_CO2)/
(1+x_H2O_gas+x_CO2);

% * Thermal conductivity dry air
lambda_air     = 0.00452+T*7.28282E-5;
% ****

Pr            = eta*c_p/lambda_air;
if Re < 1187.384382
    Nu          = ((3.66^3)+(1.66^3)*Re*Pr*(U_inner_duct/(pi*L)))^(1/3);
else
    Nu          = 0.012*(Re^(0.87)-280)*Pr^(0.4)*(1+(U_inner_duct/(pi*L))^(2/3));
end

% * Convection heat transfer coefficient dry air
alpha_air      = lambda_air*Nu/(U_inner_duct/pi);
% ****

```

```
Q_dot_fluid_wall      = alpha_air*(U_inner_duct*L)*(T-T_wall);
Q_dot_wall_ambient   = 2*pi*L*(T_ambient-T_wall)/((log(U_outer_isolation/U_outer_duct) *
/lambda_isolation)+(log(U_outer_duct/U_inner_duct)/lambda_wall));
Q_dot_wall           = Q_dot_fluid_wall+Q_dot_wall_ambient;
V_wall                = L*U_inner_duct*b_wall;
V_isolation          = L*U_outer_duct*b_isolation;
T_dot_wall            = Q_dot_wall/(
(V_wall*rho_wall*c_wall+V_isolation*rho_isolation*c_isolation);
Q_dot_fluid           = -Q_dot_fluid_wall ;
% *****
```