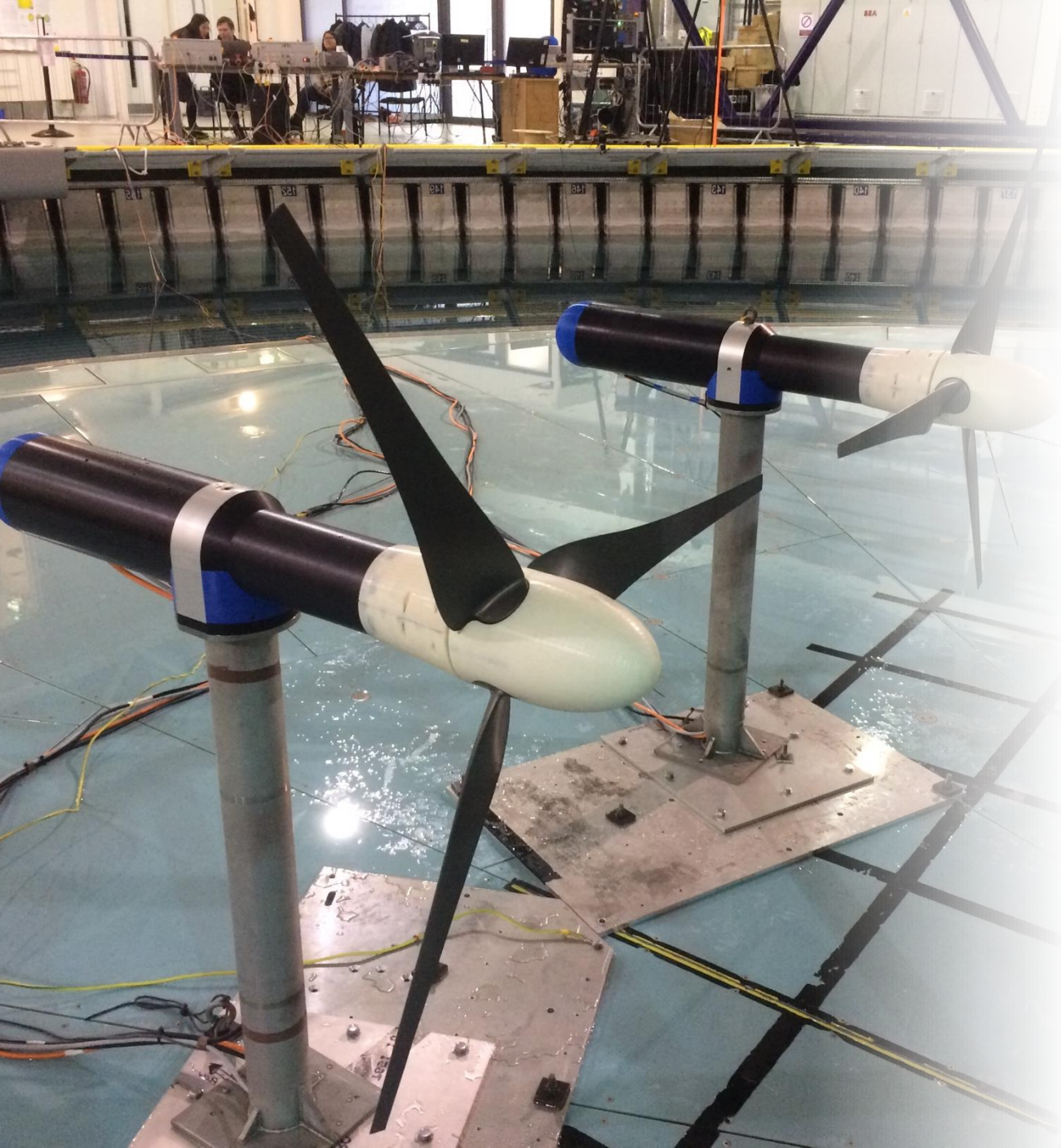


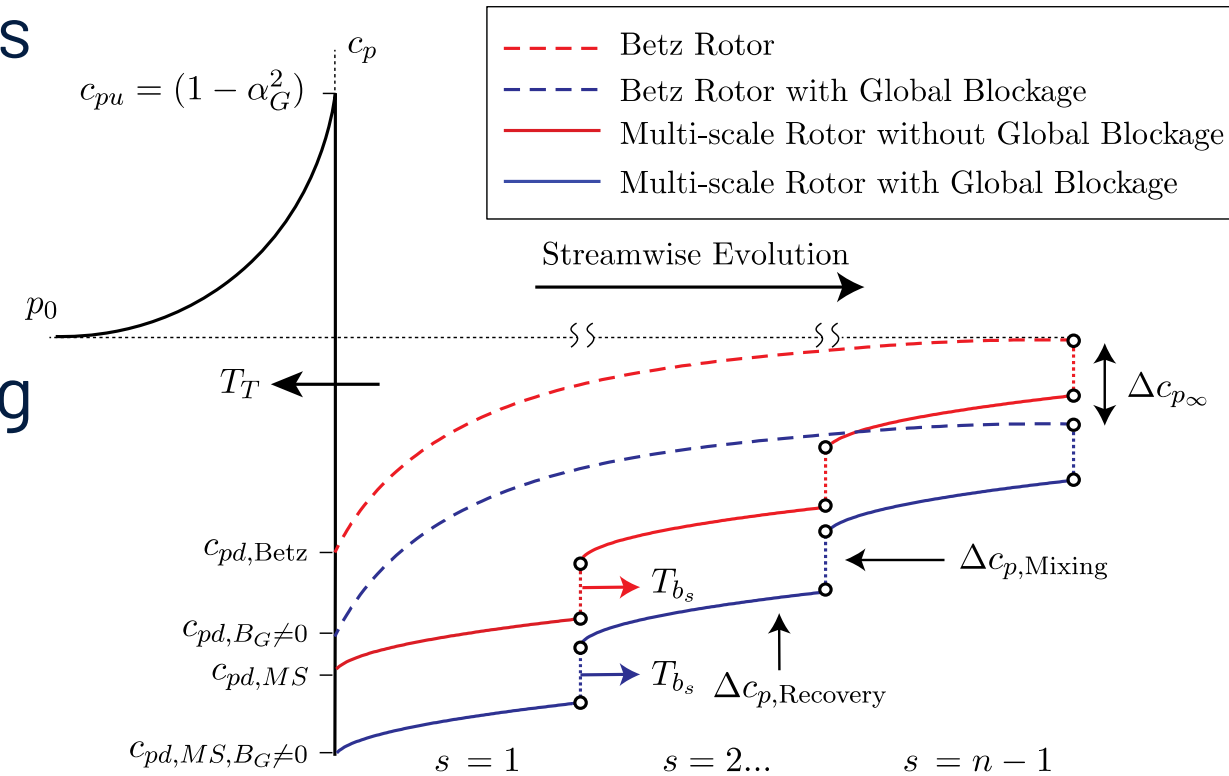


Modelling loads on closely-spaced rotors

Christopher Vogel

Modelling blockage effects

- Betz limit only applies for some cases
- Flow confinement allows a pressure drop to develop, enabling greater thrust and power on rotor
- Wake mixing is important for allowing pressure recovery in the wake
- Multi-scale mixing can allow greater pressure drops to be sustained, and thus greater power
- A lot of energy can be dissipated in the wake – trade-off between energy extraction efficiency and resource utilisation efficiency

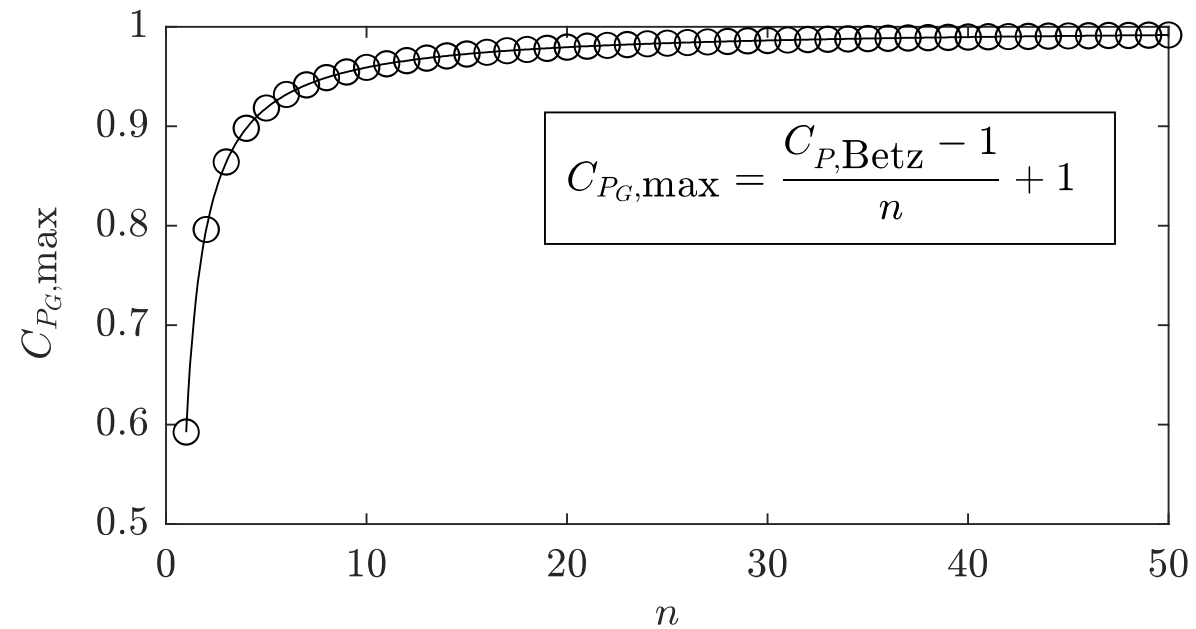


Dehtyriov et al. (2021) *J. Fluid Mech.* 927: A40

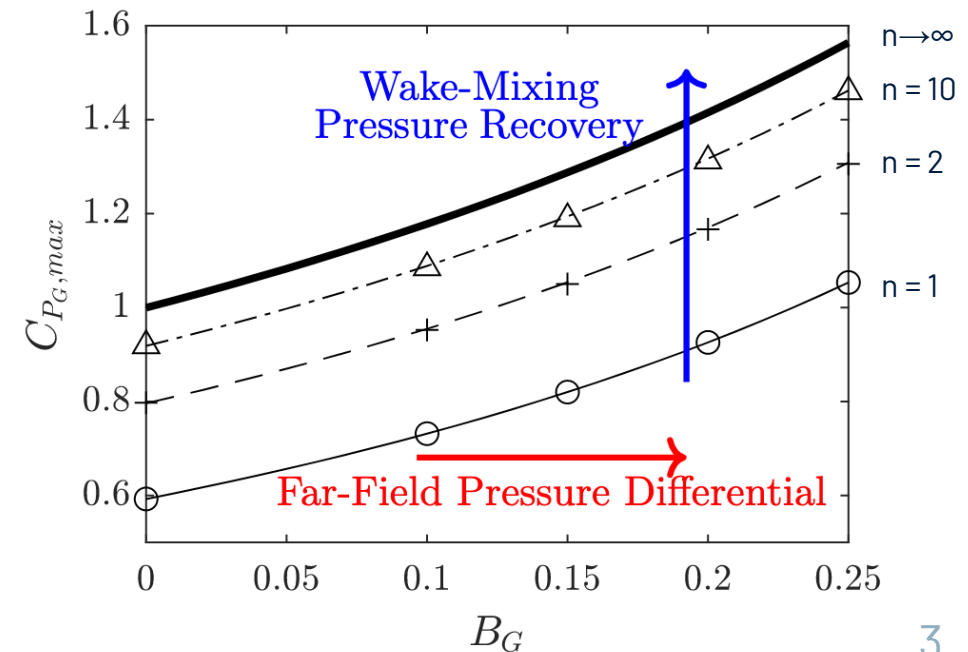
Multi-scale modelling

- Multi-scale models developed to account for differences in local and global confinement
- Max C_P tends to unity for many scales of mixing, *even when the outermost scale is unblocked*
- Max C_P is higher when the outermost scale is blocked

Can theoretical performance improvements be achieved by real turbines?

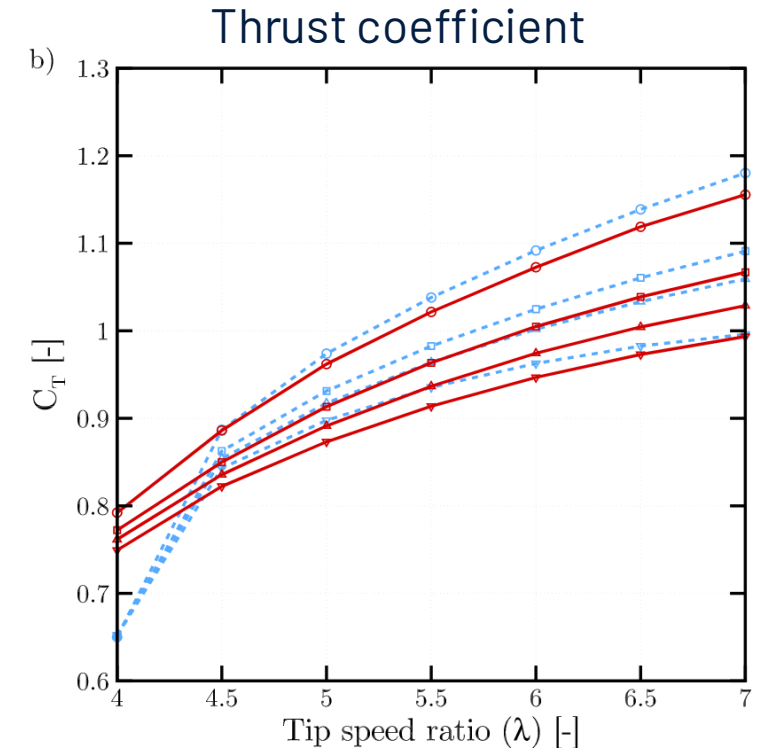
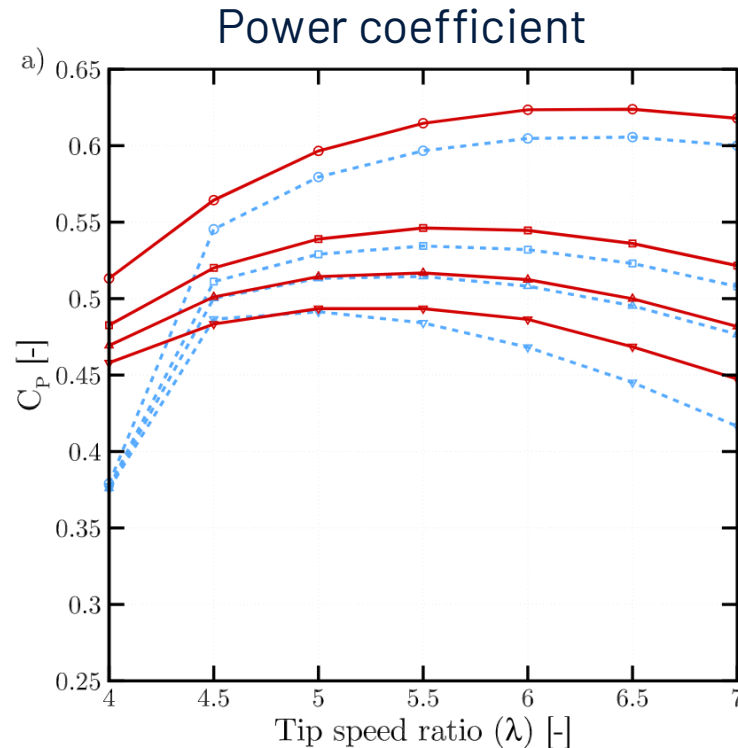


Dehtyriov et al. (2021) *J. Fluid Mech.* 927: A40



BEM + Blockage

- Inviscid blockage effects can be incorporated into rotor models e.g. BEM
- Momentum equations are modified to account for blockage
- Generally good agreement with blade-resolved simulations
- Limitations:
 - Sensitive to input lift and drag polars
 - Possible issues with high-thrust correction models

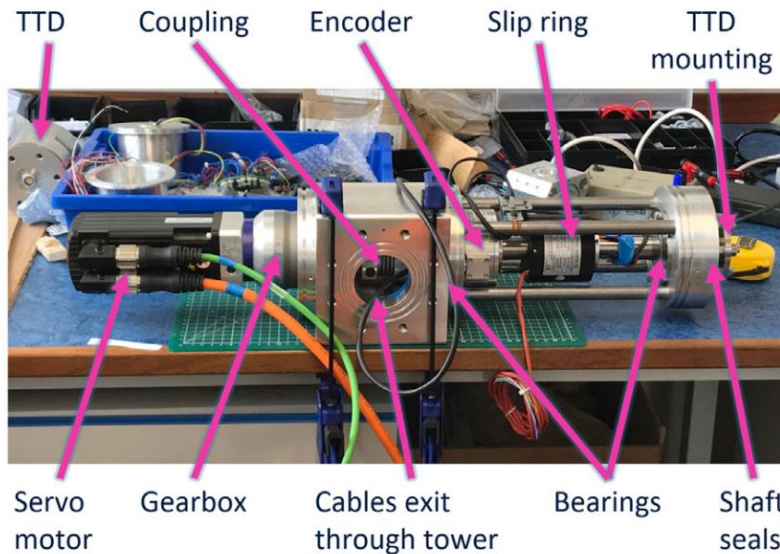
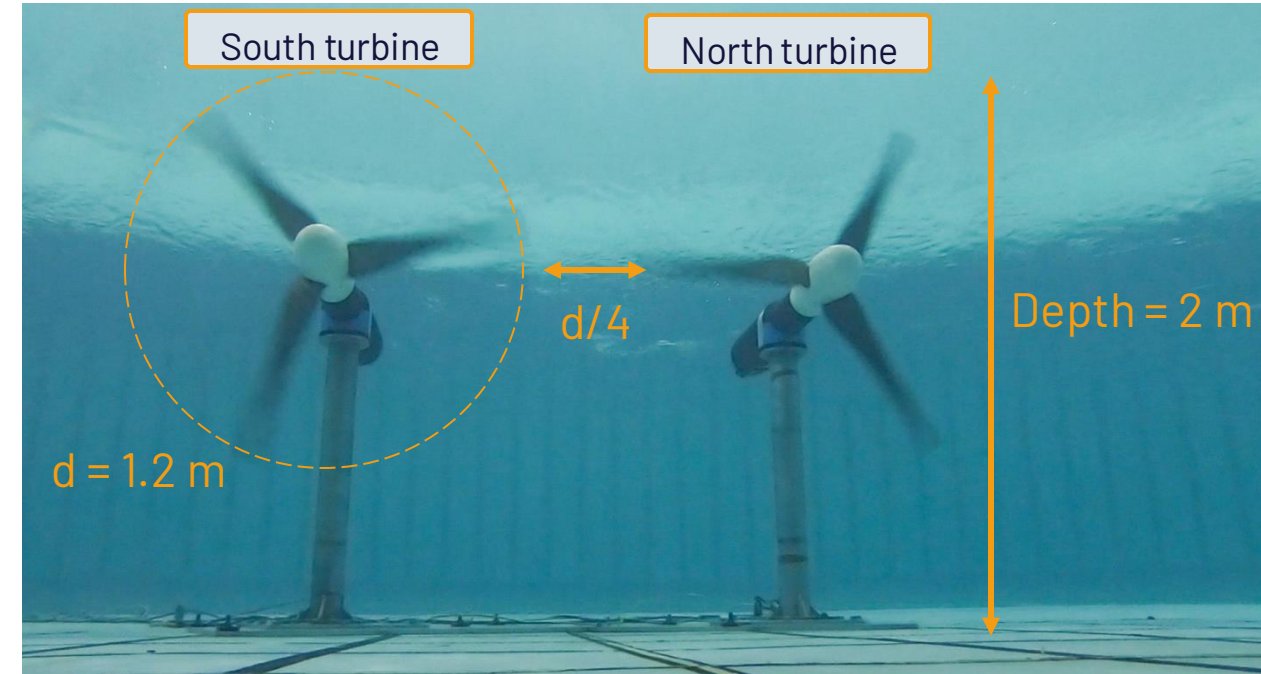


— Blade resolved ∇ B = 0.010 $\triangle$ B = 0.065 $\square$ B = 0.098 $\circ$ B = 0.196 Confined BEM —

Vogel et al. (2018) *Ocean Engineering* 169: 215-226

Rotor-rotor interactions

- Side-by-side testing of a single and two 1.2 m diameter turbines at FloWave, University of Edinburgh
- Co-rotating turbines designed for tip-to-tip spacing $s/d = 0.25$



Turbine locations

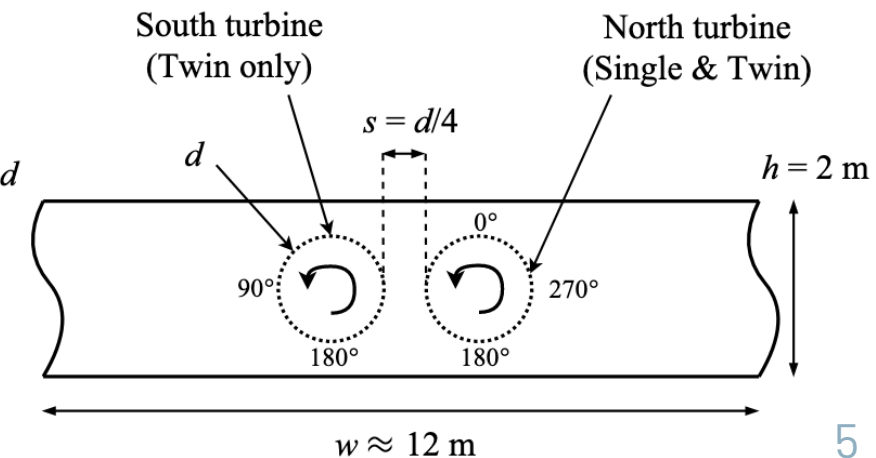
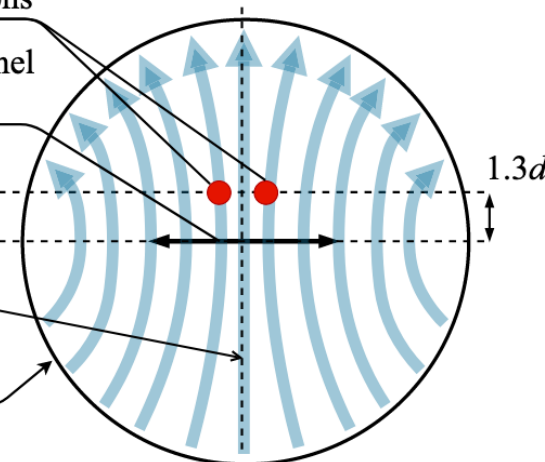
Effective channel width (w)

Rotor plane

Mid plane

Centre-line

ϕ 25 m

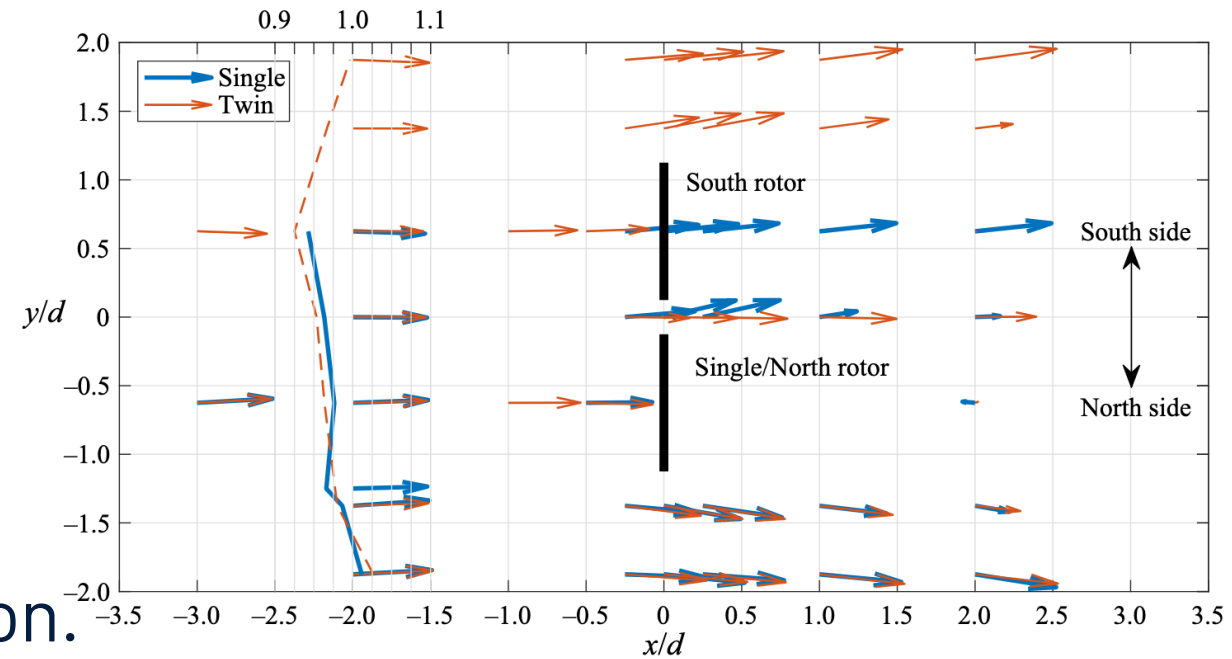


Rotor-rotor interactions

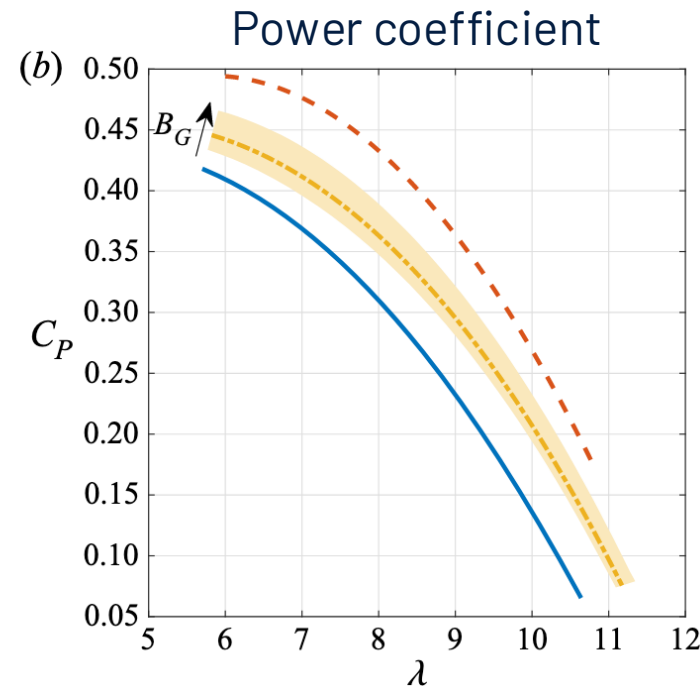
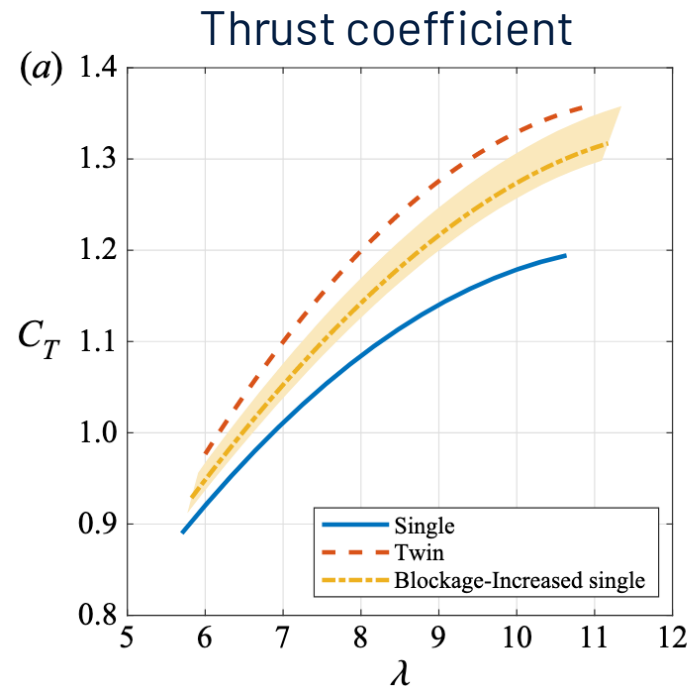
Flow

Single: flow deceleration in wake, acceleration around rotor.

Twin: acceleration observed between rotors and stronger bypass acceleration.



McNaughton et al. (2022) *J. Fluid Mech.* 943: A38
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Performance

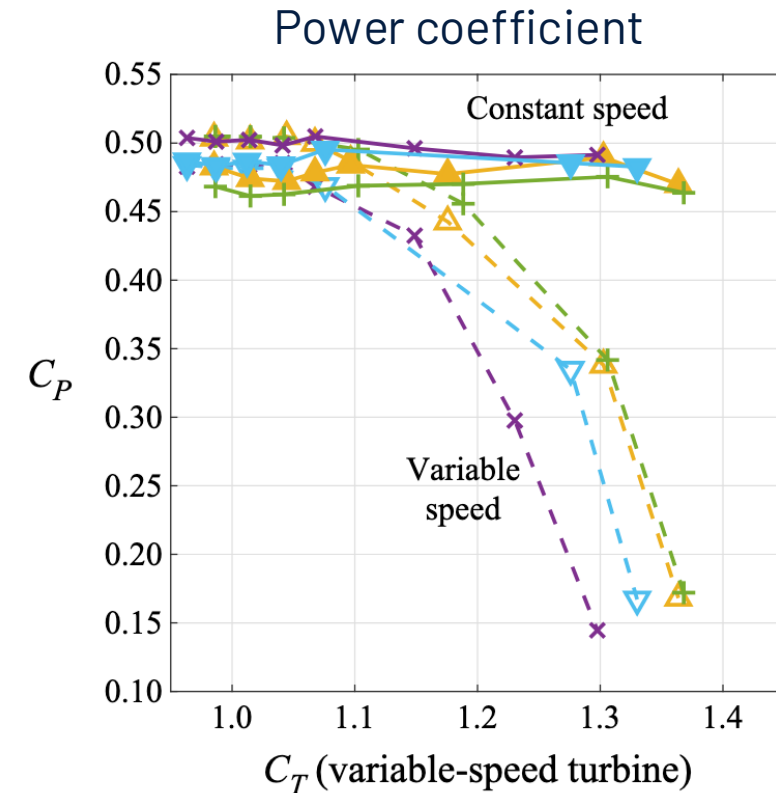
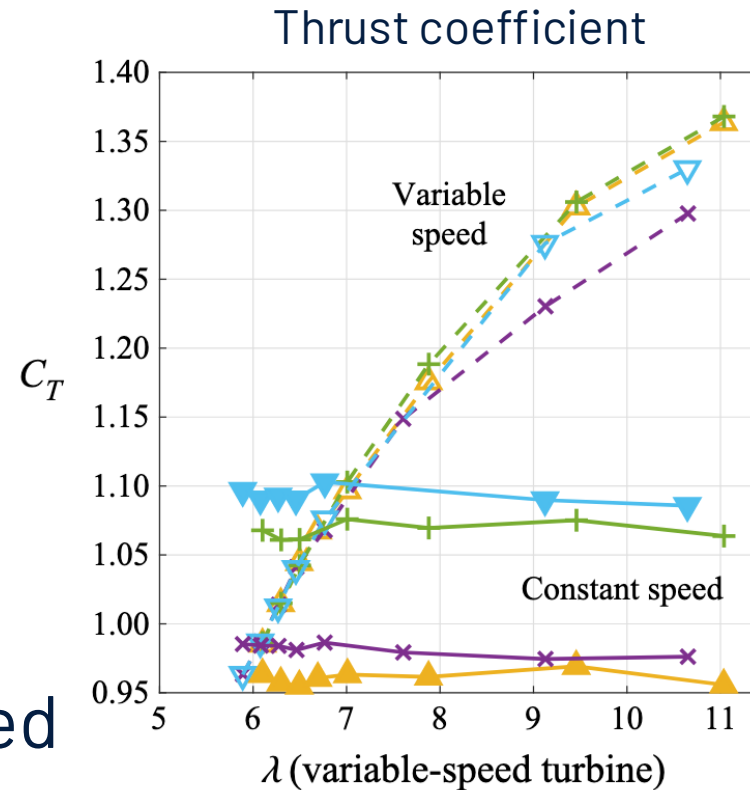
Increase in power and thrust from **single** to **twin** configurations is larger than expected from **blockage alone** – a beneficial rotor interaction occurs.

Interactions depend on turbine speed

- Interactions between rotors depend on both proximity and also how the rotors are operating
- Impact on turbine is observed due to changing operation of neighbour, even when the turbine operates at constant speed

Overall observation:

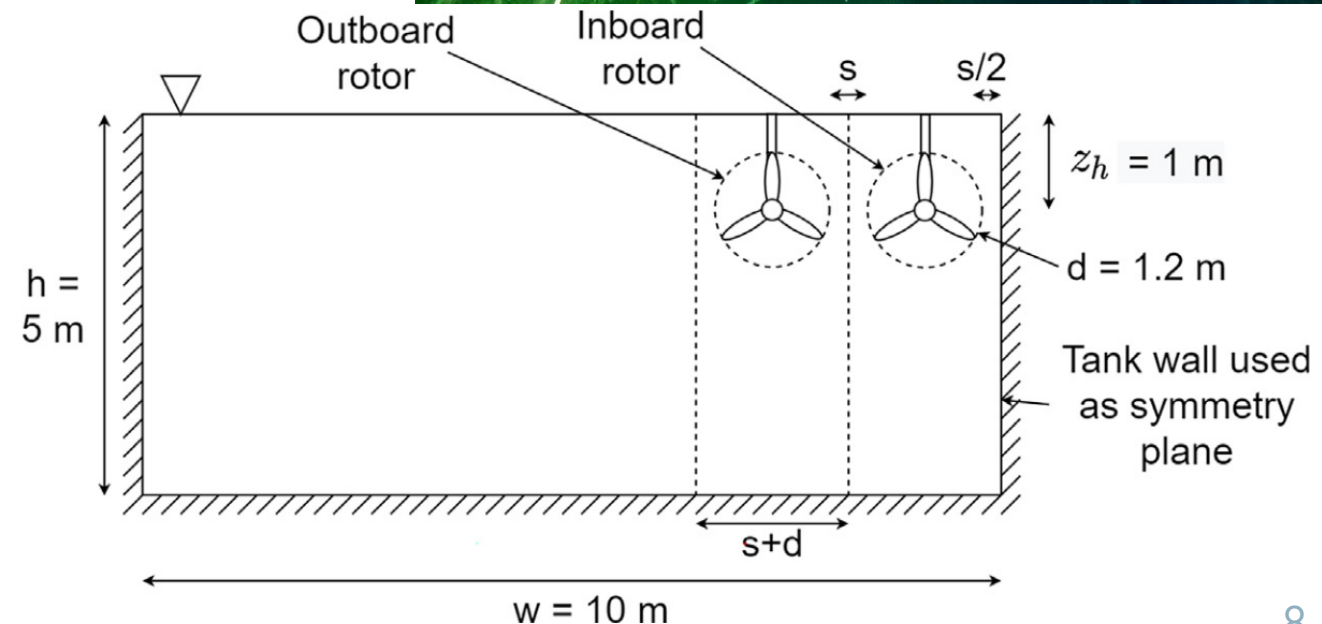
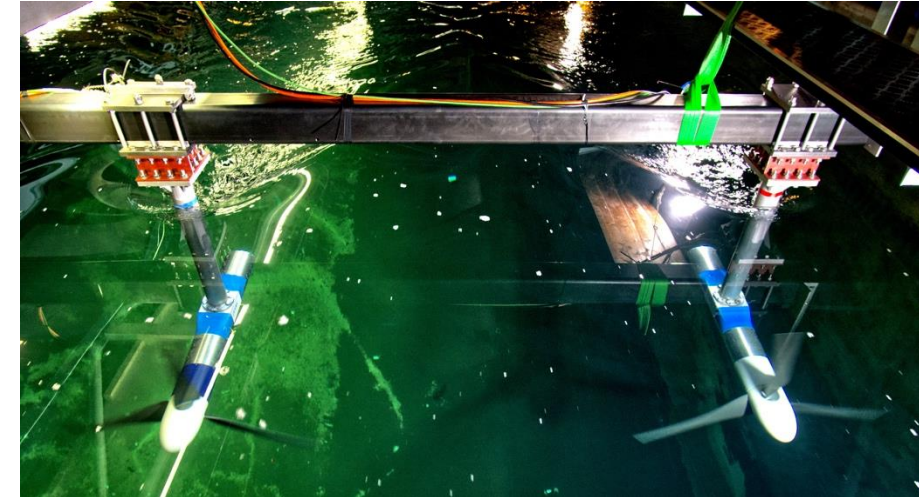
Exploiting rotor-rotor interactions led to ~20% increase in peak power with corresponding ~10% increase in thrust



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Impact of rotor spacing

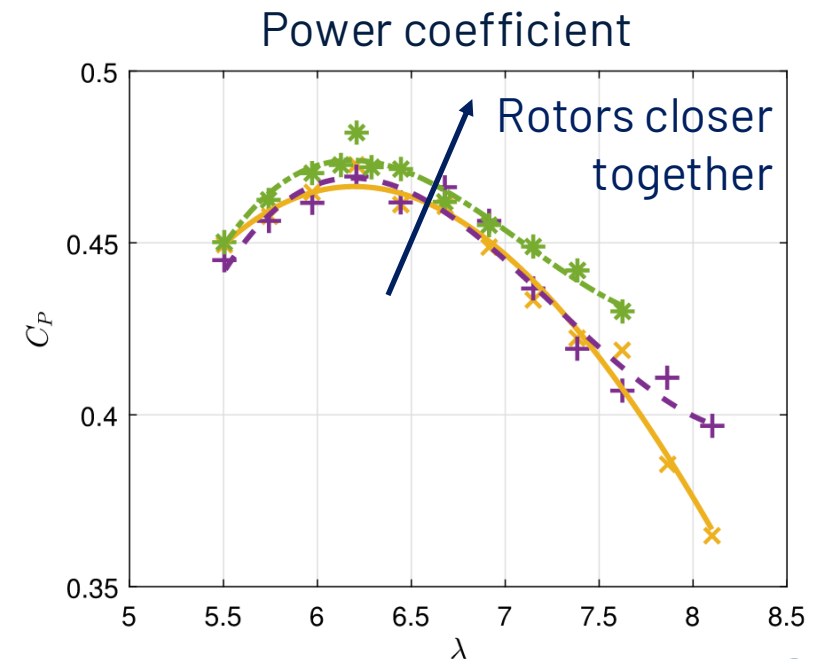
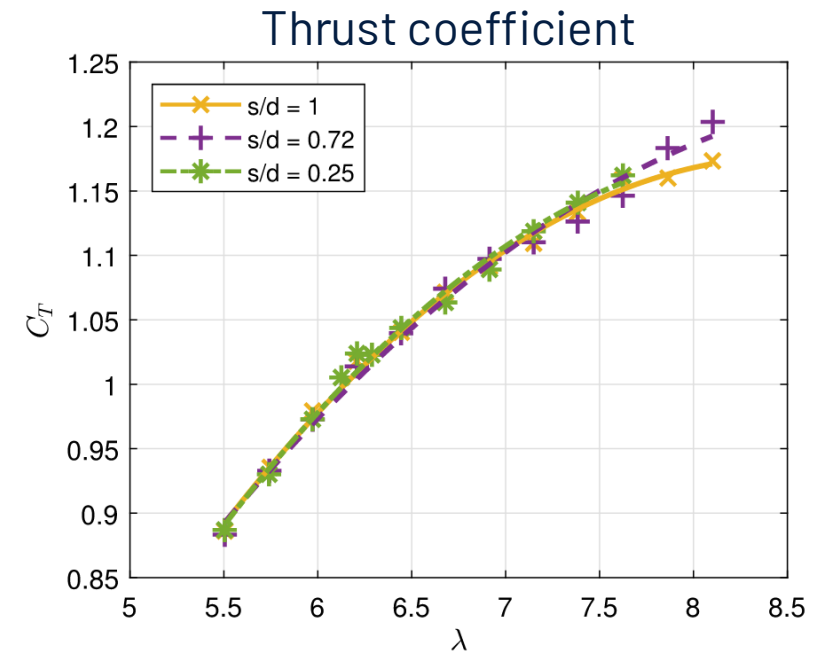
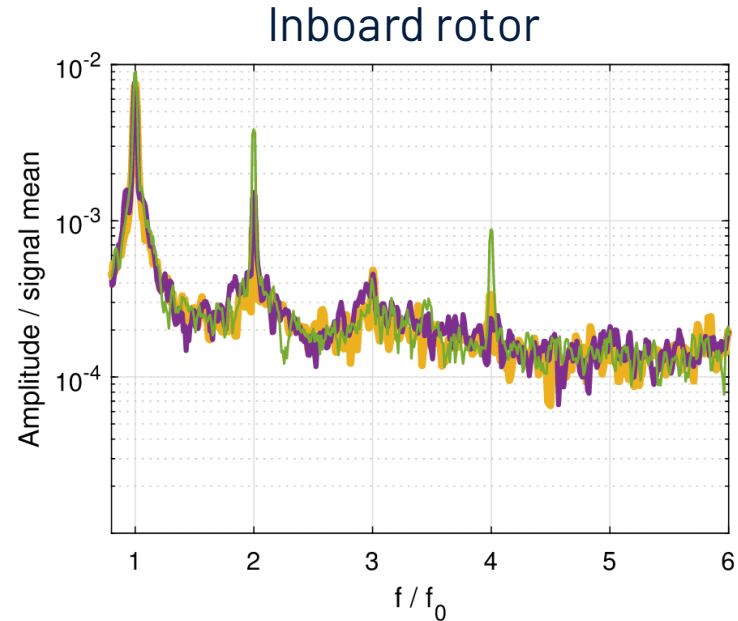
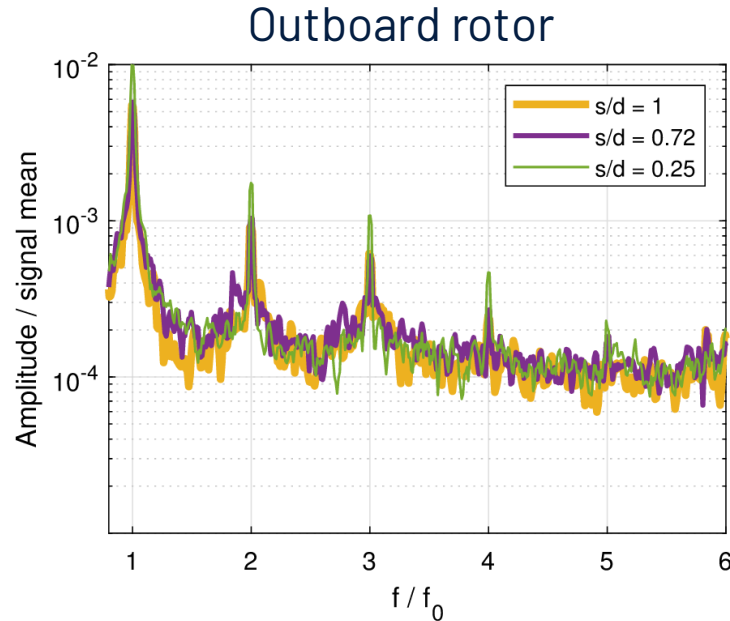
- Towing tank experiments performed at SSPA, Gothenburg
- Turbines mounted from above on a beam to allow spacing to vary
- Tank sidewall used as a symmetry plane
- Measurements:
 - Whole-rotor thrust and power
 - Blade root bending moments (flapwise and edgewise)
- Reynolds-independence above tow speeds about 0.8 m s^{-1}



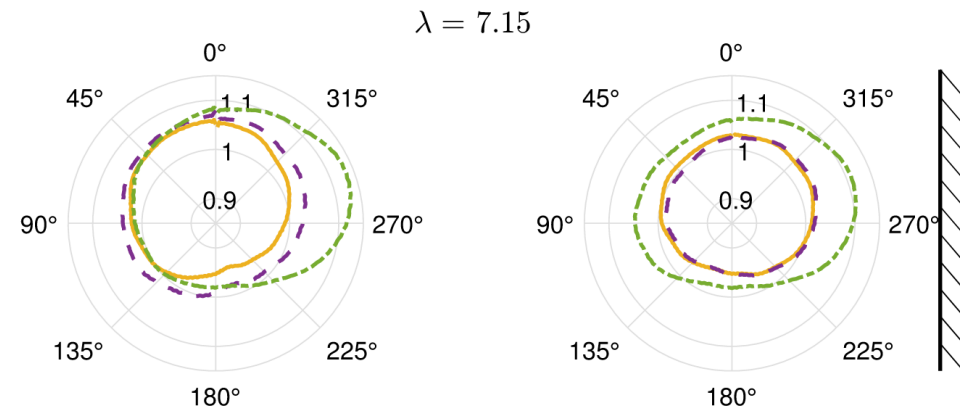
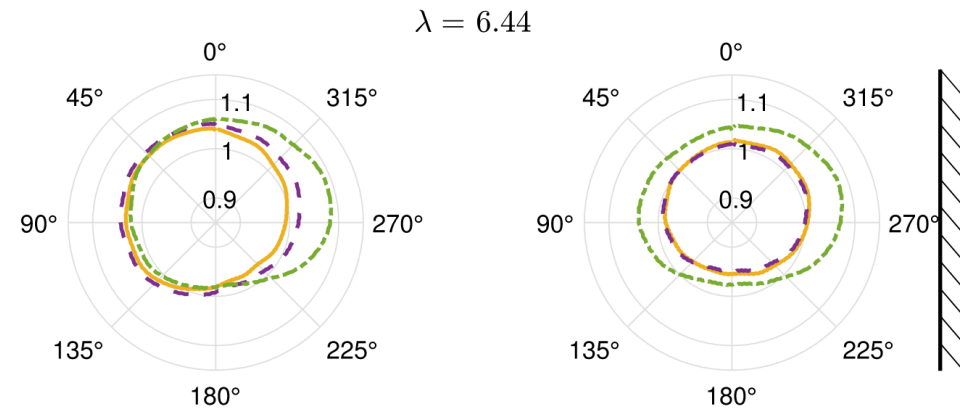
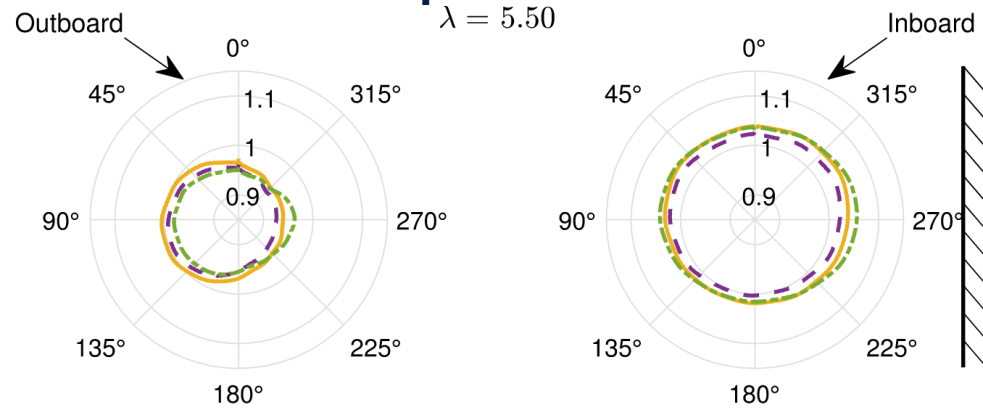
McNaughton et al. (2023) *J. Fluids Struct.* 118: 103844
H2020 MaRINET2 #3007

Impact of rotor spacing

- Decreasing tip-to-tip spacing increased peak power coefficient, little change observed for C_T
- Power of $2p$ frequency fluctuation in flapwise root bending moment increases as turbine spacing decreases – stronger interactions

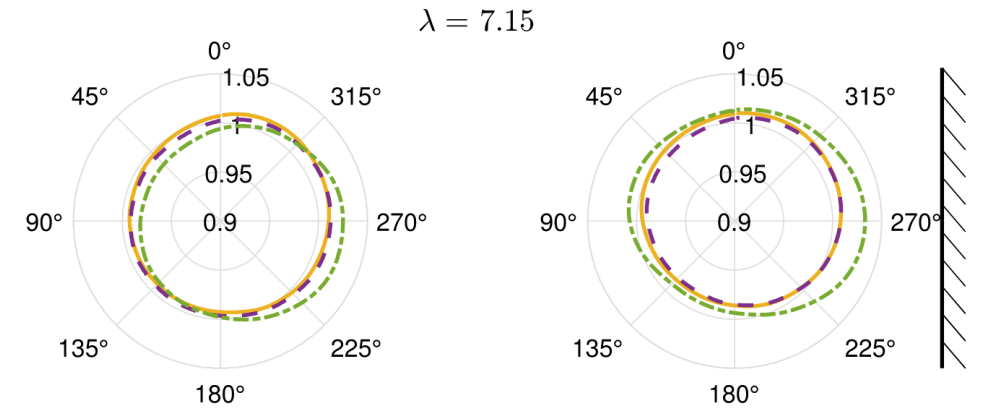
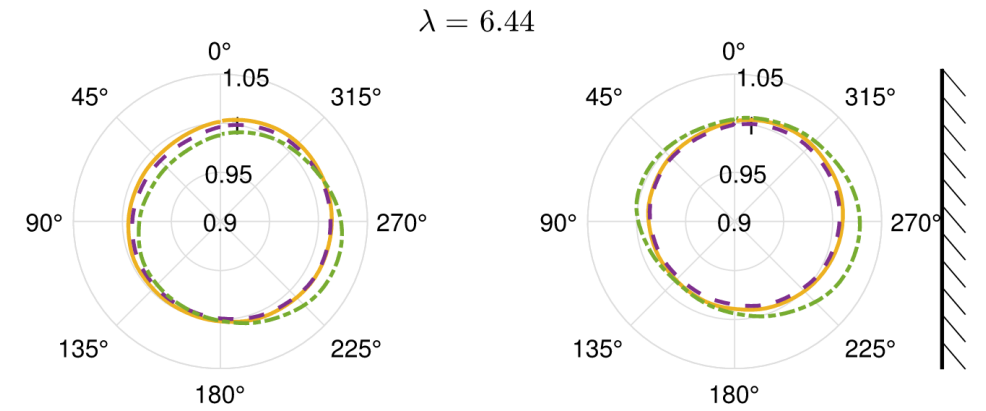
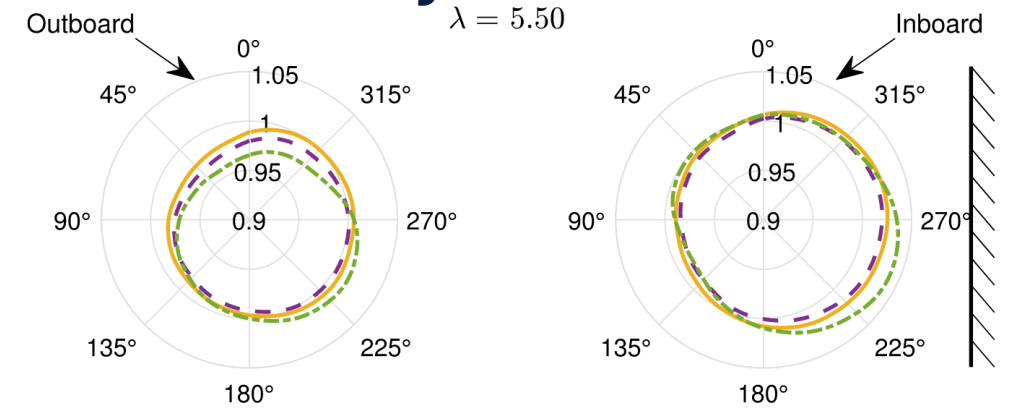


Flapwise RBM



s/d = 1 s/d = 0.72 s/d = 0.25

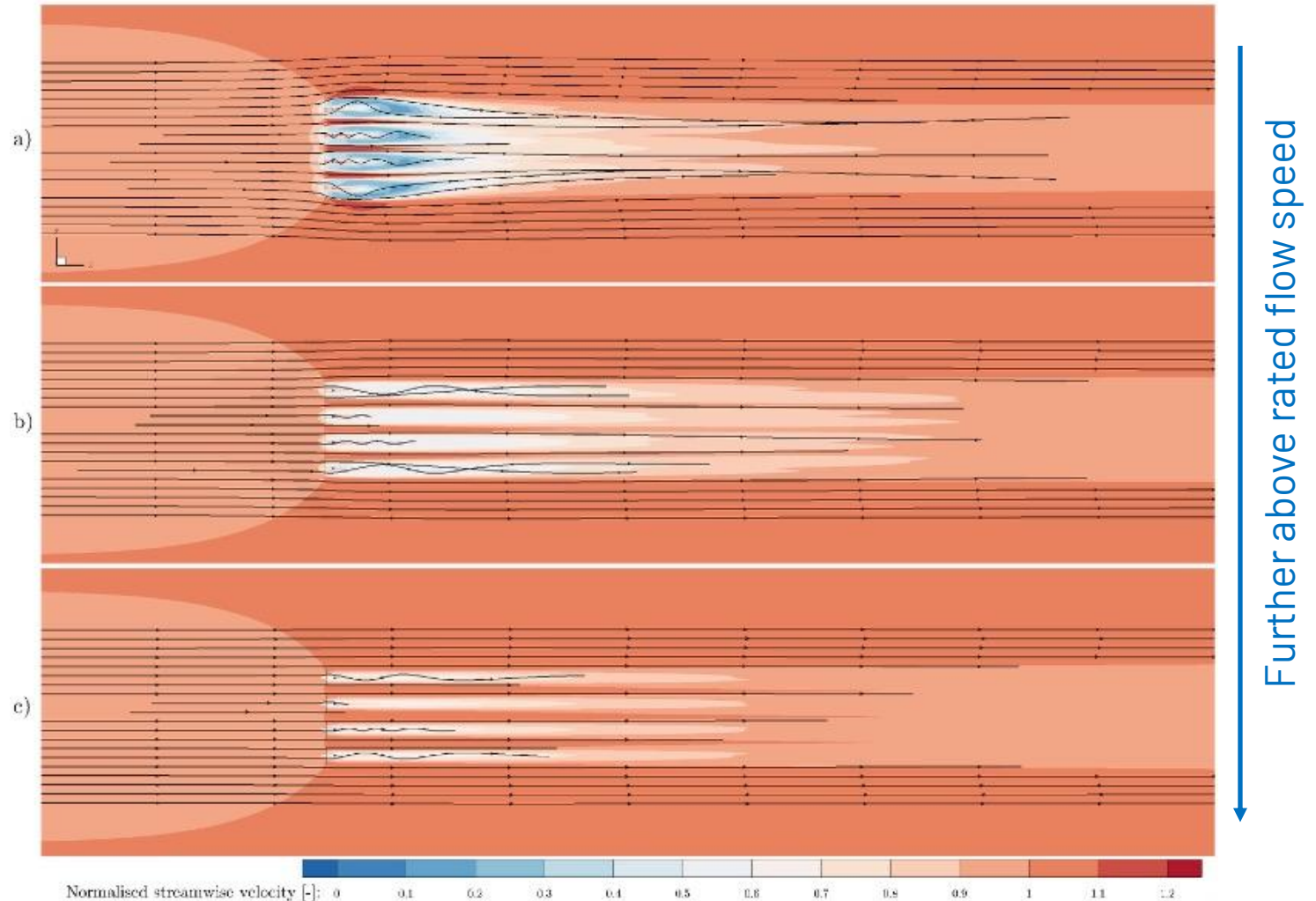
Edgewise RBM



s/d = 1 s/d = 0.72 s/d = 0.25

Rotor interactions depend on thrust

- Blockage defined as a geometric ratio, but interaction strength depends on thrust
- Above rated flow speed inter-turbine interactions can become small
- Support structures (not simulated here) may have an important influence on interactions



Conclusions

Modelling

- Far-field pressure changes drive the improved performance available to multi-scale and multi-rotor systems
- Specific corrections for BEM & actuator-based modelling of closely-spaced rotors are likely required

Loads

- Proximity to neighbouring rotors can increase power and thrust
- Interactional effects are thrust-dependent
- Close spacing of rotors enhances $2p$ load frequencies – potentially important for fatigue calculations

Thank you for your attention

christopher.vogel@eng.ox.ac.uk